

Tangent Line

Point-slope

$$y - y_1 = m(x - x_1)$$

slope

$(x_1, y_1) = \text{Point}$

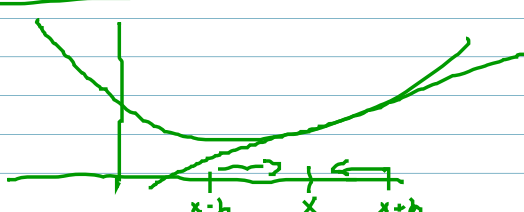
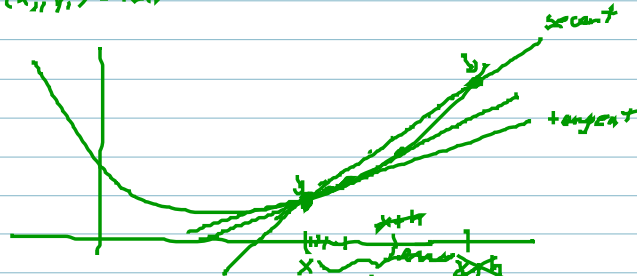


secant Line

$$\frac{y_2 - y_1}{x_2 - x_1}$$

$$m_{\text{sec}} = \frac{f(x+h) - f(x)}{x+h - x} = \frac{f(x+h) - f(x)}{h}$$

$$m_{\text{tan}} = \lim_{h \rightarrow 0} \left(\frac{f(x+h) - f(x)}{h} \right)$$



- $h = 1$
- $h = 0.5$
- $h = 0.1$
- $h = 0.01$
- $h = 0.001$

$$y = x^3 \quad (1, 1)$$

$$m_{\text{sec}} = \frac{f(x+h) - f(x)}{h}$$

$$= \frac{(x+h)^3 - x^3}{h}$$

$$= \frac{(1+h)^3 - 1}{h}$$

h	x	$x+h$	m_{sec}	h	x	$x+h$	m_{sec}
1	1	2	7	-1	1	0	-1
0.5	1	1.5	4.75	-0.5	1	0.5	1.75
0.1	1	1.1	3.31	-0.1	1	0.9	2.71
0.01	1	1.01	3.0301	-0.01	1	0.99	2.9701
→ 0.001	1	1.001	3.003001	-0.001	1	0.999	2.997001

$$m_{\text{tan}} = 3$$

$$y - 1 = 3(x - 1)$$

$$y - 1 = 3x - 3$$

$$y = 3x - 2$$

Tangent Line

Point - Slope

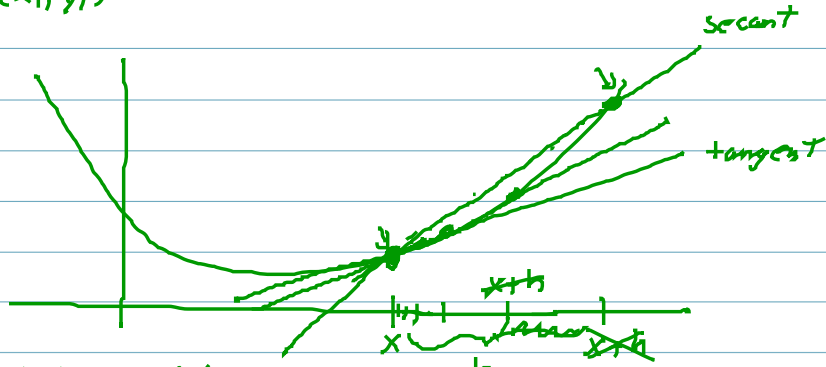
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slope

$(x_1, y_1) = \text{Point}$



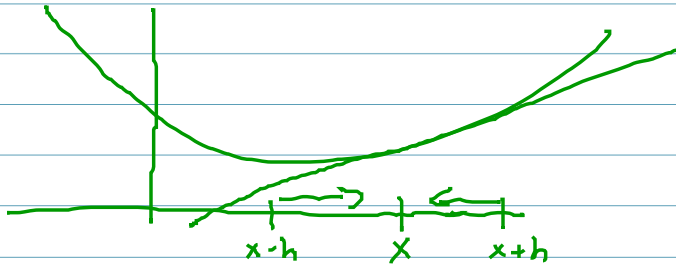
secant Line



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Velocity
Position - $f(x)$

50 miles - 1 hr \rightarrow 25 mph.
75 miles - 2 hr

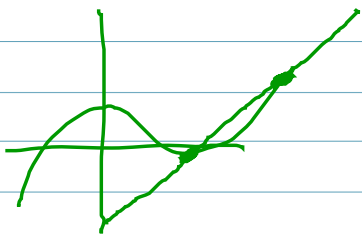
$$\text{Average Velocity} = \frac{\text{displacement}}{\text{time}} = \frac{f(a+h) - f(a)}{h}$$

$$\text{Instantaneous Velocity} = v(a) = \lim_{h \rightarrow 0} \left(\frac{f(a+h) - f(a)}{h} \right)$$

$$\text{speed} = |v(a)| = |f'(a)|$$

Derivative - slope

Rates of Change - slope



increment - change in independent variable

$$\Delta x = x_2 - x_1$$

Average rate of change of y with respect to x

$$\rightarrow \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{f(x_2) - f(x_1)}{x_2 - x_1}$$

Instantaneous rate of change of y with respect to x

$$\lim_{\Delta x \rightarrow 0} \left(\frac{\Delta y}{\Delta x} \right) = \lim_{x_2 \rightarrow x_1} \left(\frac{f(x_2) - f(x_1)}{x_2 - x_1} \right) = f'(x_1)$$